

p. 575

Indeterminate Form

$\frac{0}{0}$		$\frac{\infty}{\infty}$
$0 \cdot \infty$	0^0 0*anything=0 anything=1	1^∞ show =e
∞^0		$\infty - \infty$

Ex. 4 p. 571 can you follow?
let's make sure as a class
test question is to prove this

evaluate

$$\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x \quad | \infty$$

$$y = \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$$

$$\ln y = \ln \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x$$

$$\ln y = \lim_{x \rightarrow \infty} \ln \left(1 + \frac{1}{x}\right)^x$$

$$\ln y = \lim_{x \rightarrow \infty} x \ln \left(1 + \frac{1}{x}\right) \quad \infty \cdot 0$$

$$\ln y = \lim_{x \rightarrow \infty} \frac{\ln \left(1 + \frac{1}{x}\right)}{\frac{1}{x}} \quad \frac{0}{0} \text{ L'Hopital's}$$

$$\ln y = \lim_{x \rightarrow \infty} \frac{\ln(1+x^{-1})}{x^{-1}}$$

$$\ln y = \lim_{x \rightarrow \infty} \frac{1}{(1+x^{-1})} \cdot \frac{-x^{-2}}{-x^{-2}}$$

$$\ln y = \lim_{x \rightarrow \infty} \frac{1}{1+\frac{1}{x}}$$

$$\ln y = 1$$

$$e^1 = y$$

$$y = e$$

Stand and DeliverLimit Definition of e

8.7

$$\lim_{x \rightarrow \infty} \left(1 + \frac{1}{x}\right)^x = \lim_{x \rightarrow \infty} \left(\frac{x+1}{x}\right)^x = e$$